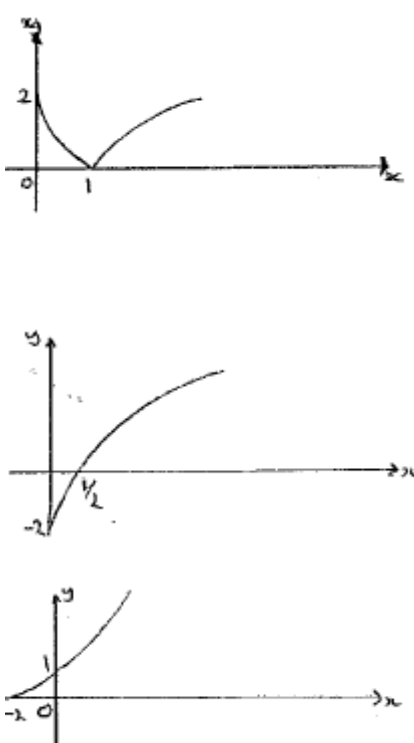


6672 Pure Mathematics P2

Mark Scheme

Question Number	Scheme	Marks
1a)	$\frac{(x-3)(x+2)}{x(x-3)}; = \frac{(x+2)}{x} \text{ or } 1 + \frac{2}{x}$ <p>B1 numerator, B1 denominator ; B1 either form of answer</p>	<p>B1,B1,B1 (3)</p>
1b)	$\frac{(x+2)}{x} = x+1 \Rightarrow x^2 = 2$ <p>M1 for equating f(x) to x + 1 and forming quadratic. A1 candidate's correct quadratic</p> $x = \pm\sqrt{2}$	<p>M1 A1√ A1 (3)</p>
2a)	 <p>Reflected in x - axis $0 < x < 1$</p> <p>Cusp + coords Clear curve going correct way Ignore curve $x < 0$</p> <p>General shaped and -2</p> <p>$(1/2, 0)$ Ignore curve $x < 0$</p> <p>Rough reflection in $y = x$</p> <p>$(0,1)$ or 1 on y - axis</p> <p>$(-2, 0)$ or -2 on x - axis and no curve $x < -2$</p>	<p>M1 A1 (2)</p> <p>B1 B1 (2)</p> <p>B1 B1 B1 (3)</p>

Question Number	Scheme	Marks
3a)	$u_2 = (-1)(2) + d = -2 + d$ $u_3 = (-1)^2(-2 + d) + d = -2 + 2d$ $u_4 = (-1)^3(-2 + 2d) + d = 2 - d$ $u_5 = (-1)^4(2 - d) + d = 2 \quad * \text{ cso}$	B1 M1 A1 A1* (4)
b)	$u_{10} = u_2 = d - 2 \quad \text{o.e.}$	their u_2 must contain d B1√ (1)
c)	$-2 + 2d = 3(-2 + d) \Rightarrow d = 4$	M1 equating their u_3 to their $3u_2$ must contain d M1 A1 (2)
4a)	$(0,4), \text{ or } x=0 \text{ and } y=4$	B1 (1)
b)	$V = \pi \int x^2 dy$	attempt use of, must have pi M1
	$x^2 = y - 4 \quad \text{or } x = \sqrt{y - 4}$	B1
	$V = (\pi) \int (y - 4) dy$	attempt to integrate M1
	$= (\pi) \left[\frac{y^2}{2} - 4y \right]$	correct integration ignore pi A1
	using limits in a changed form to give	8,4 either way but must subtract M1
	$\pi[(32 - 32) - (8 - 16)] = 8\pi \quad \text{(c.a.o)}$	A1 (6)

Question Number	Scheme	Marks
5a)	$\log 3^x = \log 5$ <p style="text-align: right;">taking logs</p> $x = \frac{\log 5}{\log 3} \text{ or } x \log 3 = \log 5$ $= 1.46 \text{ cao}$	M1 A1 A1 (3)
b)	$2 = \log_2 \frac{2x+1}{x}$ $\frac{2x+1}{x} = 4 \text{ or equivalent;}$ $2x+1 = 4x$ $x = \frac{1}{2}$ <p style="text-align: right;">4</p> <p style="text-align: right;">multiplying by x to get a linear equation</p>	M1 B1 M1 A1 (4)
c)	$\sec x = 1/\cos x$ $\sin x = \cos x \Rightarrow \tan x = 1 \quad x = 45$ <p style="text-align: right;">use of $\tan x$</p>	B1 M1, A1 (3)

Question Number	Scheme	Marks
6a)	$I = 3x + 2e^x$ Using limits correctly to give $1 + 2e$. (c.a.o.)	B1 M1 A1 (3)
b)	$A = (0, 5);$ $\frac{dy}{dx} = 2e^x$ Equation of tangent: $y = 2x + 5; c = -2.5$	$y = 5$ B1 B1 M1; A1 (4)
c)	$y = \frac{5x + 2}{x + 4} \Rightarrow yx + 4y = 5x + 2 \Rightarrow 4y - 2 = 5x - xy$ $g^{-1}(x) = \frac{4x - 2}{5 - x}$ or equivalent	putting $y =$ and att. to rearrange to find x . M1; A1 must be in terms of x A1 (3)
d)	$gf(0) = g(5); = 3$	att to put 0 into f and then their answer into g M1; A1 (2)

Question Number	Scheme	Marks
7a)	Complete method for DE [e.g. split triangle ADE and sin, or sine or cos rule] $DE = 4 \sin \theta$ * (c.s.o.)	M1 A1* (2)
b)	$P = 2 DE + 2EF$ or equivalent. With attempt at EF $= 8 \sin \theta + 4 \cos \theta$ * (c.s.o.)	M1 A1* (2)
c)	$8 \sin \theta + 4 \cos \theta = R \sin(\theta + \alpha)$ $= R \sin \theta \cos \alpha + R \cos \theta \sin \alpha$ Method for R , method for α need to use tan for 2 nd M $[R \cos \alpha = 8, R \sin \alpha = 4 \quad \tan \alpha = 0.5, R = \sqrt{8^2 + 4^2}]$ $R = 4\sqrt{5}$ or 8.94, $\alpha = 0.464$ (allow 26.6), awrt 0.464	M1 M1 A1 A1 (4)
d)	Using candidate's $R \sin(\theta + \alpha) = 8.5$ to give $(\theta + \alpha) = \sin^{-1} \frac{8.5}{R}$ Solving to give $\theta = \sin^{-1} \frac{8.5}{R} - \alpha$, $\theta = 0.791$ (allow 45.3) Considering second angle: $\theta + \alpha = \pi$ (or 180) $-\sin^{-1} \frac{8.5}{R}$; $\theta = 1.42$ (allow 81.6)	M1 M1 A1 M1 A1 (5)

Question Number	Scheme	Marks
8a)	$f'(x) = -\frac{1}{2x^2} + \frac{1}{x}$ $f'(x) = 0 \Rightarrow \frac{-1 + 2x}{2x^2} = 0; \Rightarrow x = 0.5$	M1 for evidence of differentiation. Final A –no extras (or subst x = 0.5) M1A1 * cso (5)
b)	$y = 1 - 1 + \ln\left(\frac{1}{4}\right); = -2 \ln 2$	Subst 0.5 or their value for x in M1;A1 (2)
c)	$f(4.905) = < 0 (-0.000955), f(4.915) = > 0 (+ 0.000874)$ Change of sign indicates root between and correct values to 1 sf)	evaluate M1 A1 (2)
d)	$\frac{1}{2x} - 1 + \ln\left(\frac{x}{2}\right) = 0; \Rightarrow 1 - \frac{1}{2x} = \ln\left(\frac{x}{2}\right)$ $\Rightarrow \frac{x}{2} = e^{\left(1 - \frac{1}{2x}\right)}; \Rightarrow x = 2e^{\left(1 - \frac{1}{2x}\right)} \quad * \text{ (c.s.o.)}$	M1 for use of e to the power on both sides M1;A1 (2)
e)	$x_1 = 4.9192$ $x_2 = 4.9111, x_3 = 4.9103,$	B1 both, only lose one if not 4dp B1 (2)